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Malek Mohamed Lemkecher

2009
INTERACTIVE INTERPRETATION OF NUCLEAR LOGS
WITH FAST MODELING PROCEDURES

by

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THESIS

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INTERACTIVE INTERPRETATION OF NUCLEAR LOGS
WITH FAST MODELING PROCEDURES

APPROVED BY
SUPERVISING COMMITTEE:

__________________________
Carlos Torres-Verdín, Supervisor

__________________________
William E. Preeg, Co-Supervisor
DEDICATION

First and foremost, I dedicate this thesis to our God the Merciful, who has continuously guided me in all my motivations.

Then I dedicate the work presented in this thesis to my parents Boubaker and Bakhta, my brother Khalil, and my sister Emna for their unconditional and unique love.

Thanks to you all for supporting me throughout untold periods of time working on this research.
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I am extremely thankful to my supervisor, Dr. Carlos Torres-Verdín for his outstanding pedagogy, valuable advice and consistent support during the preparation of this research project. I hope he will be proud of me throughout future successful challenges in my career. I also express my gratitude and special thanks to Dr. William E. Preeg for graciously accepting to be the second reader of this thesis. I thank the fellows in our research group – in particular Ben Voss, Alberto Mendoza, Amir Reza Rahmani Zoya Heidari, and Jorge Sanchez – for their collaboration in the development of this project.

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Malek Mohamed Lemkecher
Austin, TX August 2009
ABSTRACT

INTERACTIVE INTERPRETATION OF NUCLEAR LOGS
WITH FAST MODELING PROCEDURES

Malek Mohamed Lemkecher, M.S.E.
The University of Texas at Austin, 2009

Supervisor: Carlos Torres-Verdín

This thesis introduces new software to interactively construct multi-layer models and bedding sequences, populate layer-by-layer properties, and enable the fast simulation of nuclear logs. The method consists of modifying simultaneously layer thicknesses and properties to rapidly simulate the outcome (nuclear logs) for comparison to field logs. I include applications which appraise the numerical simulation of gamma-ray, density, compensated neutron, and photoelectric factor logs. An analogous application for sonic modeling is considered as well which uses a modified version of Wyllie’s slowness averaging equation. The procedure is tested for the case of vertical wells and horizontal layers. Examples of application include 6 synthetic and 5 field cases. Additionally, the software is implemented in combination with other formation-evaluation procedures to
interpret resistivity and nuclear logs. Simulations of nuclear logs for synthetic models can be used to improve the assessment and interpretation of field data.

Interactive modeling and simulation of nuclear logs provides a very good agreement with field logs with an average error of 3.9%. The order of logs to be matched as well as the data available are significant factors in the accuracy of the match. Numerical simulation and matching of field logs using fast modeling procedures is a reliable method to improve the inference of static and dynamic petrophysical properties of rock formations.
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CHAPTER 1

INTRODUCTION

1.1 BACKGROUND

There are four major borehole nuclear measurements: Gamma-Ray (GR), Density, Neutron, and Photoelectric Factor (PEF). While GR and PEF primarily respond to the solid components of a rock, density and neutron logs respond to the fluid that is contained within the rock’s pore space, as well as to the solid (matrix) component. Furthermore, the GR log measures natural radioactivity, whereas the remaining three measurements are acquired with a radioactive source.

Ellis et al. (2003) proposed a design of thermal neutron tools that reveals the sensitivity of the measurements to both porosity and slowing-down length of the formation. This study has been generalized in a subsequent publication of Ellis et al. (2004) to cover the sensitivity of the same measurements to lithology, gas saturation, and presence of shale.

In order to quantify porosity and matrix lithology effects on the depth of investigation of neutron and density tools, Sherman and Locke (1975) described experimental work to study invasion effects on a formation saturated with salt water by varying fluids across different levels of invasion. Wiley and Patchett (1994) approached the problems of invasion and differences in radial length of investigation using a deterministic diffusion code to model thermal neutron and porosity measurements with different formations. Furthermore, Tittle (1992) employed an analytical version of the diffusion theory to quantify the effect of invasion on nuclear measurements for different
radial lengths of invasion. Such simulations considered both sources and sensors as infinitesimal objects.

Watson (1984) introduced the concept on Monte Carlo-derived differential sensitivity functions for detector responses due to Compton and photoelectric gamma-ray interactions. This concept led to fast nuclear log simulation with the use of linear sensitivity functions. Afterward, Aristodemou et al. (2006) developed a method to diminish the computational time needed in the simulation of well-logging nuclear measurements using the energy group optimization theory.

In an earlier work, Radtke et al. (2007) showed that the resolution of density and neutron logs is governed by the source-to-detector distance. Several methods have been investigated, notably the Monte Carlo N-Particle (X-5 Monte Carlo Team MCNP, 2003) code, to simulate borehole nuclear measurements.

Mendoza et al. (2007) developed fast approximate numerical procedures making use of Monte Carlo-derived spatial flux-scattering functions (FSFs) for specific tool configurations, which have been used in this thesis.

Wyllie et al. (1956) proposed an averaging equation for sonic slowness. In this thesis, we adapt this equation to make it relevant for both siliciclastic and carbonate sequences.

1.2 PURPOSE

The main objective of this thesis is to allow the user to match field logs with numerical simulations by interactively modifying geometrical and petrophysical properties of layers. Figure 1.1 describes this objective in flow-chart relations that emphasize the connection between the lithological/fluid composition and the numerical simulation of logs.
This thesis also implements FSF simulation on user-defined beds, with the goal of producing results analogous to those of field logs. The procedure first consists of specifying solid and fluid constituents of a set of consecutive layers. I then populate petrophysical properties, such as bulk density, migration length, and others associated with solid and fluid constituents. Fluid density is derived from temperature and depth by means of Peng-Robinson’s (1976) equation of state. Calculation of nuclear properties is performed with Schlumberger’s SNUMPAR code (McKeon and Scott, 1989). Subsequently, FSF-based simulations of nuclear well logs are performed and results compared to borehole measurements. This functionality is unique since existing software products, such as ELAN, do not take into account bed boundaries, invasion, or response functions. The field cases treated in this thesis demonstrate the effectiveness of log matching, following the interactive modeling and FSF simulations.

The thesis also intends to effectively combine the Borehole Resistivity Module, Borehole Sonic Module, and Formation Evaluation Toolbox (UTAPWeLS user guide, 2009) in the interpretation of layer-by-layer petrophysical properties. Figure 1.2 describes the generic flow chart of UT Petrophysical and Well Log Simulator, emphasizing the role of this thesis.
Figure 1.1: Objective of the thesis represented in flow-chart relations that emphasize the connection between the lithological/fluid composition and numerical simulation of logs.
Figure 1.2: Generic flowchart of UT Petrophysical and Well-Log Simulator, emphasizing the role of this thesis.

1.3 ORGANIZATION OF THIS THESIS

This thesis is organized as follows:

Chapter 2 details the characteristics of the Bed Properties Tool introduced in the thesis. It also describes the modeling algorithm, as well as the computations behind it.

Chapter 3 details the characteristics of the Nuclear Simulation Module that follows the modeling of the beds, consisting of FSF-based simulations and the options included with them.
Chapter 4 analyzes the results of several synthetic and field case studies. These cases contain different situations encountered in practice, such as carbonate, siliciclastic, and thinly-bedded formations. Different methods are considered in order to establish the final assessments, emphasizing the manual iterative procedure used to match field logs, full log analysis, and initial guess.

Chapter 5 summarizes the most important conclusions stemming from the modeling and simulation exercises.
CHAPTER 2

BED PROPERTIES TOOL

This chapter provides a detailed description of the Bed Properties tool used for the modeling of horizontal beds, as well as of the computations behind the modeling algorithm.

2.1 FUNCTIONALITY

The Bed Properties tool is a set of interfaces used to facilitate the lithological description of a chosen bed sequence, as well as of some of its petrophysical properties. This description can be specifically defined for different beds within the same sequence, as well as its fluid properties, which may change radially. Once the sequence has been defined, a final interface allows the user to simulate the proposed definition in order to compare it to the corresponding field logs. This process will be then repeated in order to refine the result (Figure 2.1).

The definition of bed boundaries can be either done arbitrarily or using the Master Curve Selection tool that permits the user to designate a field log in order to simulate it. This generation may be performed by squaring the designated log (gamma-ray log for example) and setting a shale index value limit so that it separates sands from shales for the case of siliciclastic sequences.
Figure 2.1: Flow chart describing two options which can be defined for simulation of nuclear logs. Input data can be either user-defined beds, or raw field data. In the former case, the manual iterative procedure is identified with a dashed line.

The manual iteration process can be performed at two levels: either by returning to the bed-boundary definition in order to add more layers or split a previously defined layer, or by reviewing the bed-property definition at the palette level (Figure 2.2). In either case, nuclear simulations have to be performed once more to quantify the resulting changes, and improve the match to field logs.

2.2 OUTLINE

Bed properties are defined with a selection palette that allows the user to assign different parameters to each consecutive bed. These attributes are classified into components: Matrix, Fluid, Shale, and Common Petrophysical/Fluid properties (Figure 2.2).
Figure 2.2: Snapshot of the selection palette. Each section is highlighted with a different color. The user enters his/her own definition for each boundary-defined bed. This step is accessible again if the user wishes to make modifications following the simulation results. Once nuclear properties have been defined for each bed, the user can perform numerical simulations. The Common Petrophysical/Fluid Properties section allows the user to enter the temperature gradient in the absence of a temperature log, shale structure, and water salinity.
2.2.1 Matrix

The matrix selection permits the user to enter different combinations of each solid matrix component of a bed based upon mineral constituents. Minerals vary from mica, calcite, etc. After the minerals are entered, the software checks whether their respective fractions add up to one, thereby verifying that the user has entered all the specific constituents.

2.2.2 Fluid/Gas

The fluid selection allows the user to input different combinations of fluid/gas contained in the rock’s pore space. Constituents can be fresh water, brine, and/or hydrocarbon. Hydrocarbons predefined in the software range from methane (CH$_4$) to Eikosane (C$_{20}$H$_{42}$). All isomers are included since their densities vary as well. Similar to the solid selection when the user validates their entry, the software verifies whether the sum of the fluid saturations adds up to one. Since brine is a generic term for saline water, the user can specify its salt concentration in order to readjust the corresponding fluid density.

2.2.3 Shale

The shale selection permits users to enter both the solid and fluid components of any type of shale. The solid part of the shale is generally silt (quartz) and clay, while the fluid part can be anything previously mentioned in the main fluid selection. Users also enter the porosity of the shale such that the corresponding molecular properties are properly weighted.
2.2.4 Common Petrophysical/Fluid Properties

The last section contains all other relevant definitions related to any chosen bed. Non-shale porosity and volumetric shale concentration are required to ensure the accuracy of the calculations undertaken by the software. Temperature is necessary for the simulation of density and neutron measurements, and can be either entered manually, selected from a field log (if available), or calculated from two different depths with their corresponding temperature values. Salinity may be required if the connate water saturation is considerably high, and can be entered either in NaCl, KCl, or CaCl₂ volumetric concentrations (ppm). If one of the two latter options is used, it will get automatically converted to NaCl salinity based on a coefficient chart.

2.3 COMPONENT PROPERTIES

A detailed data base of pure mineral properties is required to simulate gamma-ray and sonic logs. Tables 2.1 and 2.2 describe the set of parameters used in most of the cases discussed in this thesis (Mineral Mnemonics, SIS). The data base has been separated into solid and fluid composition since the nature of its respective properties is different. Furthermore, the fluid data set exists in both generic mode (common definitions) and specific mode where one can attribute properties to distinct chemical formulas. Knowing that these values may vary slightly due to packing and diagenesis, one may have to adjust the minerals and their volumetric concentration in order to improve the simulation results. This can be done in the Solid Component Properties (Figure 2.3a) and the Generic Fluid Component Properties (Figure 2.3b).
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<th>Chemical formula</th>
<th>Density $(\rho$, g/cc)</th>
<th>Potassium $(K$, %)</th>
<th>Uranium $(U$, ppm)</th>
<th>Thorium $(Th$, ppm)</th>
<th>Sonic slowness $(\Delta t$, μs/ft)</th>
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Table 2.1: Summary of solid properties defaulted in the Palette. Values can be customized based on specific field characteristics.
<table>
<thead>
<tr>
<th>Name</th>
<th>Chemical formula</th>
<th>Sonic slowness ($\Delta t, \mu s/ft$)</th>
<th>Critical pressure ($P_c, \text{ atm}$)</th>
<th>Critical temperature ($T_c, \text{ K}$)</th>
<th>Acentric factor ($\omega$)</th>
<th>Molecular weight ($M, \text{ g/mol}$)</th>
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<tr>
<td><strong>Generic Fluids</strong></td>
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<td>Sour Gas</td>
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<td>45.35</td>
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</tbody>
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Table 2.2: Summary of fluid properties defaulted in the Palette. Complex fluid values cannot be modified since each property is unique for each element.
Figure 2.3a: Snapshot of the Solid Component Properties. Each component is associated with its own defined chemical formula, density, spectral gamma-ray values, and acoustic transient time.

Figure 2.3b: Snapshot of the Generic Fluid Component Properties. Each component is associated with its defined chemical formula, acoustic transient time, critical pressure and temperature, acentric factor, and molecular weight.
2.4 DATA TREATMENT

After the software checks for input errors, the user has a valid input for a given bed. For the case of gamma-ray measurements, the software recalls from a data base the radioactivity proportion for each mineral input. Radioactivity is measured in parts-per-million (ppm) of Uranium and Thorium, and fraction (%) of Potassium. Amounts are re-evaluated after adding the values from the Solid Components of the Shale selection. In addition to the solid data base, the software uses a data base that contains four properties for each fluid/gas: critical pressure ($P_c$), critical temperature ($T_c$), acentric factor ($\omega$), and molecular weight ($M$). These four properties, in addition to bed temperature and bed pressure, are necessary to calculate the corresponding fluid density using Peng-Robinson’s method. Bed pressure is assumed to be equivalent to the hydrostatic pressure at a particular depth. Once the fluid/gas densities are retrieved, the software scales the density based on the rock’s composition and calculates the corresponding neutron migration length (via SNUPAR). These two parameters, in addition to the previously averaged radioactivity spectral values, are finally stored for access by the second part of the software where numerical simulations take place.

Apart from the data to be used for nuclear simulation, the Palette includes a sonic P-wave slowness model. Similarly to density weighted averaging, this model is generated by combining each bed’s composition. We use Wyllie’s (1956) averaging equation for this purpose:

$$\frac{1}{\Delta t_b} = \frac{\phi}{\Delta t_f} + \frac{1-\phi}{\Delta t_s},$$

(2.1)

where $\phi$ is porosity (fraction) and $\Delta t$ is sonic slowness (time per distance) of the pure bulk, fluid, and solid ($\Delta t_b$, $\Delta t_f$, and $\Delta t_s$, respectively). Since we will be dealing with both siliciclastic and carbonate sequences, we adapted Wyllie’s equation to read as
\[ \Delta t_b = \phi \cdot \Delta t_f + (1 - \phi - C_{sh}) \cdot \Delta t_s + C_{sh} \cdot [\phi_{sh} \cdot \Delta t_{sh,f} + (1 - \phi_{sh}) \cdot \Delta t_{sh,s}], \quad (2.2) \]

where the subscripts “sh,f” and “sh,s” designate the shale fluid and solid properties, respectively, and \( C_{sh} \) is the corresponding volumetric concentration.
CHAPTER 3

SIMULATION OF BOREHOLE NUCLEAR MEASUREMENTS

This chapter describes the characteristics of the Nuclear Simulation Module, which comes into play after beds have been defined. These simulations are FSF-based and can be adjusted with certain options.

3.1 DESCRIPTION OF THE MODULE

The Borehole Nuclear Module is a user-friendly graphical interface for the simulation and interpretation of nuclear measurements (Figure 3.1). These measurements are performed based on the data previously generated by the Palette. Numerical modeling is based on iterative, linear-refinement approximations (Mendoza, 2009).
3.2 FUNCTIONALITY

Simulations performed by this module concern GR, density, compensated neutron, and PEF. Specifically, GR simulation is performed from the Thorium, Uranium and Potassium concentrations. Compensated neutron logs are simulated from migration lengths. For the case of simulation of density and PEF measurements, we choose density of the formation as the weighted nuclear sensitivity parameter. All these parameters are related to the cross-section and therefore to the tool response (count rate).

Prior to performing the GR simulation, the three spectral models are weighted for each separate bed using the formula
\[ GR = a_c \cdot Th + b_c \cdot U + c_c \cdot K \, , \]

where \( GR \) is the weighted gamma ray value (gAPI); \( Th \) and \( U \) are the thorium and uranium concentration (part per million), respectively; \( K \) is the potassium concentration (%); and \( a_c \), \( b_c \), and \( c_c \) are their corresponding coefficients, which are defaulted to be 2.71, 6.51, and 14.23, respectively. These values may differ based on the formation, but are constant within the same sequence. Once the weighted GR value is obtained, FSF-based simulations are performed by the module (Mendoza et al., 2007).

Among the options available for density and compensated neutron simulations, the user can refine the results by adding a linear iterative refinement, which takes into account the FSF spatial variations. This refinement takes into account the variations of the response functions that are due to local perturbations of energy-dependent cross-section (Mendoza, 2009). This option, on the other hand, will increase the Central Processing Unit (CPU) time of the simulations.

Based on the type of simulation selected, certain cross-plots will be available for display. They consist of Density vs. Neutron (Figure 3.2), Potassium vs. Thorium, PEF vs. Th/K, and PEF vs. Density. Each cross-plot is overlaid by its corresponding interpretation chart (Log Interpretation Charts, SIS), which helps the user to diagnose and verify the model lithology.
Figure 3.2: Example of Density ($\Phi_D$, limestone porosity units) vs. Neutron ($\Phi_N$, limestone porosity units) cross-plot distinctly colored for each layer.

If the compensated neutron simulation is selected, one has to specify the chosen lithology, which can be sandstone, limestone or dolomite. The user should specify both mudcake thickness and mudcake density in order for the simulations to account for environmental effects, as this applies to density simulation as well.

Finally, all the calculations will vary inversely with time and accuracy based on the chosen sampling rate. To secure the fastest response, the sampling rate should be set to half the thickness of the thinnest defined bed.
CHAPTER 4

CASE STUDIES

This chapter evaluates the previously defined methods on several case studies, including both synthetic and field data sets. Synthetic cases consist of making different composition changes on the same initial set of layers, while field cases are performed on different reservoirs.

4.1 SYNTHETIC CASE

In this section, I initially define generic beds with significant variations of mineral/fluid composition. Subsequently, a series of changes is applied to the synthetic case to quantify the resulting variations on the numerically simulated logs.

The synthetic case (Figure 4.1) consists of six beds: the top five beds consist of approximately equal-thickness layers of pure limestone, shale, sandstone, dolomite, and an additional layer of limestone. All these beds are initially saturated with water. The bottom layer consists of a thicker shale bed.
Figure 4.1: Description of the synthetic model with corresponding simulated logs. Track 0: Lithology log: Limestone (green), Shale (orange), Sandstone (yellow), and Dolomite (blue). Track 1: Bed boundaries and environmentally corrected gamma-ray simulated log (ECGR, gAPI). Track 2: Simulated neutron (NPHI, limestone porosity units) and density logs ($\rho_a$, g/cm³). Track 3: PEF simulated log (barn/electron) and sonic slowness log ($V_{P,formation}$, μs/ft). Track 4: Depth track (ft).

All the beds are defined with equal porosity, knowing that the porosity of shale beds is bound. Note that neutron simulations were performed assuming limestone porosity units.

4.1.1 Changing the fluid composition

The first sensitivity analysis to consider is the change of fluid composition: I reduce water saturation by 10% and substitute the rest with gas (CH₄), assuming that the water left is at irreducible conditions. When compared to the initial log (Figure 4.2), I observe the following changes:
- The density decreases by an average of 0.65 g/cm$^3$ while remaining constant within shale beds.
- The neutron simulation decreases by an average of 21% while remaining constant within shale beds.
- The sonic model decreases by an average of 82 $\mu$s/ft while remaining constant within shale beds.
- The GR simulation remains unaffected.

Figure 4.2: Simulated logs for the synthetic model with 90% of methane in fluid saturations. Track 0: Lithology log: Limestone (green), Shale (orange), Sandstone (yellow), and Dolomite (blue). Track 1: Bed boundaries and environmentally corrected gamma-ray simulated log (ECGR, gAPI). Track 2: Simulated neutron (NPHI, limestone porosity units) and density logs ($\rho_o$, g/cm$^3$). Track 3: PEF simulated log (barn/electron) and sonic slowness log ($V_{P,formation}$, $\mu$s/ft). Track 4: Depth track (ft).
4.1.2 Including an additional layer

This time, I introduce a layer of anhydrite with low radioactivity content above the bottom layer. As expected, the GR simulation across that layer is negligible (almost 0 gAPI), whereas the neutron and density simulations yielded relatively considerable changes (Figure 4.3). In fact, the neutron density was set to 12% (limestone porosity units) while the recorded density was 2.8 g/cm³.

![Simulated logs for the synthetic model with an additional layer of anhydrite. Track 0: Lithology log: Limestone (green), Shale (orange), Sandstone (yellow), Dolomite (blue), and Anhydrite (red). Track 1: Bed boundaries and environmentally corrected gamma-ray simulated log (ECGR, gAPI). Track 2: Simulated neutron (NPHI, limestone porosity units) and density logs (\(\rho_a\), g/cm³). Track 3: PEF simulated log (barn/electron) and sonic slowness log (\(V_p,_{\text{formation}}\), μs/ft). Track 4: Depth track (ft).](image)
4.1.3 Modifying porosity

In this case, I increase the total porosity of all the beds from 20% to 35%. The updated results (Figure 4.4) indicate an increase of 33 μs/ft in the sonic log and 0.21 g/cm³ in the density, while GR and PEF are barely altered. While all the sonic and the density logs experience a constant increase, the neutron simulation exhibits a decrease of 12.8% (limestone porosity units) instead. Note that all these changes are observed in non-shale beds.

Figure 4.4: Simulated logs for the synthetic model after modifying the overall porosity. Track 0: Lithology log: Limestone (green), Shale (orange), Sandstone (yellow), and Dolomite (blue). Track 1: Bed boundaries and environmentally corrected gamma-ray simulated log (ECGR, gAPI). Track 2: Simulated neutron (NPHI, limestone porosity units) and density logs (ρₜ, g/cm³). Track 3: PEF simulated log (barn/electron) and sonic slowness log (Vₚ,formation, μs/ft). Track 4: Depth track (ft).
4.1.4 Including an additional mineral in the bulk solid composition

Unlike previous modifications that dealt with pure minerals in each bed, I set the volumetric concentration of quartz equal to 30% in each layer (Figure 4.5). This time, sonic and density logs are readjusted mainly at shale beds, while the remaining layers are marginally affected. The sonic log exhibits an increase of 30 μs/ft while the density log decreases by 0.39 g/cm³.

![Simulated log of the synthetic model with a modified matrix composition](image)

**Figure 4.5:** Simulated log of the synthetic model with a modified matrix composition. Track 0: Lithology log: Limestone (green), Shale (orange), Sandstone (yellow), and Dolomite (blue). Track 1: Bed boundaries and environmentally corrected gamma-ray simulated log (ECGR, gAPI). Track 2: Simulated neutron (NPHI, limestone porosity units) and density logs (ρ_a, g/cm³). Track 3: PEF simulated log (barn/electron) and sonic slowness log (V_{P,formation}, μs/ft). Track 4: Depth track (ft).
4.1.5 Adding thinly-bedded layers

In this final simulation experiment, I include a sequence of adjacent thin beds of sand and shale. The outcome of the simulation (Figure 4.6) emphasizes the importance of the choice of simulation sampling rate, since it is not capable of resolving the thinly-bedded layers, specifically in depths ranging from 17932 ft to 17924 ft. It is imperative to choose a sampling rate smaller than the thinnest bed in the defined model in order to obtain a reliable result.

Figure 4.6: Simulated logs for the synthetic model with a sequence of thin beds of sand and shale. Track 0: Lithology log: Limestone (green), Shale (orange), Sandstone (yellow), Dolomite (blue), and a sequence of thin beds of shale and sand (brown). Track 1: Bed boundaries and environmentally corrected gamma-ray simulated log (ECGR, gAPI). Track 2: Simulated neutron (NPHI, limestone porosity units) and density logs ($\rho_a$, g/cm$^3$). Track 3: PEF simulated log (barn/electron) and sonic slowness log ($V_{P,\text{formation}}$, $\mu$s/ft). Track 4: Depth track (ft).
4.1.6 Salinity effect on nuclear logs

Concerning this example, a different synthetic model was used:

- I construct 8 water-filled adjacent beds of thicknesses ranging from 8 to 13 ft.
- I set the same petrophysical properties for each layer but vary the volumetric concentration of NaCl in their connate water from 0 to 100 kppm.
- I choose pure limestone for the matrix composition and assume a negligible change of temperature.

Figure 4.7 describes the effect of changing the salinity of connate water on nuclear logs, notably PEF, Density, and Neutron.

I observe that the higher the salinity, the lower the values of density, neutron, and PEF. I also observe that the change is more noticeable whenever $C_w$ exceeds 5 kppm. This is an important observation to consider whenever there is an offset between simulated and field logs, which would indicate the need of an adjustment of the water salinity of the layers.
Figure 4.7: Simulated logs for a synthetic case with a sequence of limestone beds of equal petrophysical properties but different salinities. Track 1: Bed boundaries, migration length ($L_{\text{formation}}$, ft), and PEF (barns/electron) logs. Track 2: Simulated neutron (NPHI, limestone porosity units) and density logs ($\rho_a$, g/cm$^3$). Track 3: Volumetric concentration of NaCl in connate water ($C_w$, ppm).
4.2 Field Studies

In this section, I test the full procedure on field examples. The cases contain descriptive situations encountered in practice, such as carbonate, siliciclastic, thinly-bedded, and offshore formations. Based on the type of data available, different methods are considered in order to establish the final assessments, emphasizing the manual iterative procedure, initial guess, and full log analysis.

4.2.1 Carbonate Formation

The field logs to be interpreted correspond to a carbonate sequence (Figure 4.8a & 4.8b, shown in blue). This sequence describes a carbonate reservoir that contains a high amount of secondary porosity. The carbonate sediments mainly consist of thinly- to thickly-bedded dolomite with complex depositional and diagenetic features (Miranda, 2008). Beds were initially deposited from grain-rich up to mud-rich carbonates. Subsequently, they underwent diagenesis that significantly modified their fabric, texture, and petrophysical properties.

I first define bed boundaries where I identify a considerable change in the composition based on GR variations. The minimum variation considered for detecting a bed boundary is 75%, and the number of beds is approximately 13. Then, for each bed separately, the palette is used to input the composition based on log analysis. After all layers definitions are entered, nuclear-log simulations are executed. Gamma-ray, density, and neutron logs are plotted to be compared to their corresponding field logs. If the simulations (Figures 4.8a and 4.8b, shown in red) at certain depth intervals do not agree with field logs then an iterative refinement step is added, which consists of redefining bed properties by either partitioning them into smaller beds or by redefining the compositions and volumetric concentrations of the bed.
Figure 4.8a: Field and simulated logs for the carbonate example. Track 1: Depth track (ft). Track 2: Bed boundaries and caliper (ft). Track 3: Lithology (fraction): orthoclase (grey), quartz (yellow), biotite (green), dolomite (purple), limestone (black), glauconite (orange), illite (gold), water (blue), shale water (light blue), oil (red). Track 4: GR (gAPI). Track 5: Density (g/cm³). Track 6: Neutron (limestone porosity units). Track 8: PEF (barn/electron).
Figure 4.8b: Field and simulated logs for the carbonate example. Track 1: Depth track (ft). Track 2: Bed boundaries and caliper (ft). Track 3: Lithology (fraction): orthoclase (grey), quartz (yellow), biotite (green), dolomite (purple), limestone (black), glauconite (orange), illite (gold), water (blue), shale water (light blue), oil (red). Tracks 4 to 8: High-Resolution Laterolog Array Tool from shallow to deeper radial lengths of investigation (Ω.m).
Figure 4.8c: Spatial distribution of resistivity and water saturation. Track 1: Depth track (ft). Track 2: Lithology (fraction): orthoclase (grey), quartz (yellow), biotite (green), dolomite (purple), limestone (black), glauconite (orange), illite (gold), water (blue), shale water (light blue), oil (red). Track 3: GR (gAPI). Track 4: High-Resolution Laterolog Array Tool (Ω.m). Track 5: Water saturation (fraction).
Results show that the percentage of clay in layers that exhibit high gamma-ray is relatively high; quantitatively, in the top layer, I observe 41% illite and 18% glauconite, while the bottom layer exhibits 52% of illite and 24% glauconite content. Layers that have the lowest gamma-ray values mainly consist of dolomite (71% dolomite for the depth interval 11712 to 11728 ft). I also observed that the highest values of neutron porosity were located in the top (32% limestone porosity units) and bottom (28% limestone porosity units) layers. The reason behind this effect is the high hydroxyl content in the clay included in those layers. The average relative error in the PEF log is 3%, which implies a reliable match.

Concerning the simulated resistivity logs (Figure 4.8b), I observe a constant under-estimation of the resistivity values in the upper quarter of the formation, and a constant over-estimation in the interval that lies between 11728 ft and 11750 ft. The most probable reason behind these offsets is due to the fact that resistivity logs were the last to be matched. The colored spatial distribution of the simulated resistivity and water saturation results (Figure 4.8c) indicates that the drilling mud was water-base, since the radial distribution interval from 11692 ft to 11699 ft shows a lower resistivity from the borehole wall to the radial distance of 1 ft. Finally, I observe a deep WBM-filtrate invasion in the interval from 11728 ft to 11750 ft.

4.2.2 Siliciclastic Formation

The purpose of this example is to apply a similar matching procedure to a siliciclastic formation. The field logs to be interpreted were acquired in a mixed rock sequence, predominantly siliciclastic, as included in the calculated lithology log. Based on the core description, the sequence is a sandy limestone, half of which includes calcite
with a trace of dolomite. Moreover, the limestone is interspersed as thin siltstone beds. Figure 4.9a is a previous lithology work that I use as initial guess.

A procedure similar to that of the previous example is used for detecting bed boundaries, since both sequences belong to the same wellbore but are situated at different depths. Water saturation ($S_w$) was computed through Archie’s equation (1942) i.e.,

$$S_w = \left[ \frac{a}{\phi^m} \cdot \frac{R_{w}}{R_t} \right]^{1/n}.$$

Where $a$ is tortuosity factor, $R_w$ is connate water resistivity, $\phi$ is effective porosity, and $m$ and $n$ are cementation and saturation exponents, respectively. For this field case, I assumed values of 1.84 and 2 for the cementation and saturation exponents respectively, while the tortuosity factor is taken as 1.

As in the previous example, I did not attempt to match all the small log variations but rather concentrated on matching the general trends for each layer. Figure 4.9b describes the match between the field logs (in blue) and simulated models (in red). Note that the abrupt change around the depth of 11,146 ft signaled in the caliper log caused an error in the GR log; therefore, I did not include it in the matching procedure.

In layers with substantial amounts of limestone (80% volumetric fraction), the density log measures an increase of 0.3 g/cm$^3$, while the neutron log measures a decrease of 12% (sandstone porosity units). Moreover, the simulated PEF exhibits a larger increase in the layers with higher volumetric fraction of limestone (from 11070 ft to 11075 ft, from 11105 ft to 11117 ft, and from 11123 ft to 11145 ft). The opposite trend takes place for the case of the sonic log.

From this formation, I conclude that the high concentration of limestone in a siliciclastic sequence results in high measured values of density and PEF logs, and low
measured values of neutron and sonic logs. Hence, the iterative procedure makes it easier to detect such a combination of minerals.

Figure 4.9a: Lithology log used as the starting point for the assessment of lithology and petrophysical properties of layers. Left column represents the user-defined layers. Track 1: Bulk mineral composition. Track 2: Fluid composition.
Figure 4.9b: Field and simulated logs for the siliciclastic example. Track 1: Depth track (ft). Track 2: Bed boundaries and caliper (ft). Track 3: Lithology (fraction): quartz (yellow), limestone (red), illite (grey), water (blue), shale water (light blue). Track 4: GR (gAPI). Track 5: Density (g/cm³). Track 6: Neutron (sandstone porosity units). Track 7: PEF (barn/electron). Track 8: Sonic slowness (μs/ft). Track 9: High-Resolution Laterolog Array Tool of deepest radial length of investigation (Ω.m).
4.2.3 Case with available spectral GR logs

The purpose of this field example is to enhance the agreement between simulated and observed field logs by using spectral GR logs in the initial approach. Unlike previous cases, the study of this sequence was entirely based on logs and a minimal amount of core data. Hence, full log analysis had to be performed to calculate petrophysical properties. The availability of the spectral GR logs was beneficial to initialize the lithological composition. The thorium vs. potassium cross-plot (Figure 4.10) helped to determine the types of clay existing in the formation. In this case, I inferred the presence of smectite, kaolinite and some chlorite along different beds.

Figure 4.10: Left: Track 1: Depth track (ft). Track 2: GR log (gAPI) and petrophysical bed boundaries. Right: thorium vs. potassium cross-plot for field example 3 used to infer types of clay contained in the sequence. Beds are numbered from top to bottom.
The log shown in **Figures 4.11a** and **4.11b** show the initial model defined based on results imported from the log analysis into the palette. Moreover, the previous cross-plot was combined with the GR log, which allowed me to differentiate between shale and sand beds, as well as to define the types of clay existing in each individual bed.

I first observe 8 major shale beds, in which the amount of bound water is high (12% volumetric concentration), while hydrocarbon is contained between these layers. I also observe a clear shale baseline in the simulated resistivity log, which is Schlumberger’s Micro-Spherically Focused Conductivity Tool. As emphasized earlier in field case No. 1, the neutron log exhibits a large increase (27% sandstone porosity units) whenever the clay content is considerable (70% clay concentration). In addition, low porosity in clays resulted in high sonic slowness values (an average increment of 18 μs/ft).

Once the model was built, minor adjustments were needed on the spectral GR of minerals and clays, since these values can vary based on different geographic locations. Thorium, potassium and uranium values can be improved using the log values at pure shale sequences.

Based on this example, I conclude that the availability of spectral GR logs greatly helps to assess clay mineralogy, and hence in achieving an improved match between simulated and field logs.
Figure 4.11a: Field and simulated logs for example No. 3. Track 1: Depth track (ft). Track 2: Bed boundaries and caliper (ft). Track 3: Lithology (fraction): quartz (yellow), smectite (grey), kaolinite (brown), illite (purple), shale water (dark blue), water (blue), hydrocarbon (red). Track 4: GR (gAPI). Track 5: thorium concentration (ppm). Track 6: uranium concentration (ppm). Track 7: potassium concentration (%). Track 8: Apparent Spherically Focused Resistivity (Ω·m).
Figure 4.11b: Field and simulated logs for example No. 3. Track 1: Depth track (ft). Track 2: Bed boundaries and caliper (ft). Track 3: Lithology (fraction): quartz (yellow), smectite (grey), kaolinite (brown), illite (purple), shale water (dark blue), water (blue), hydrocarbon (red). Track 4: GR (gAPI). Track 9: Density (g/cm$^3$). Track 10: Neutron (sandstone porosity units). Track 11: Sonic slowness (μs/ft).
4.2.4 Case with an illustrated manually-iterated procedure

The sequence analyzed in this case is a North Louisiana’s tight-gas sand (Heidari et al., 2009). Despite the lack of core data, we know that this sequence was drilled with water-based mud (WBM). Resistivity logs show a significant separation, which indicates deeply invaded beds; nonetheless, I observe a substantial cross-over between neutron and density logs. This cross-over indicates the existence of residual gas saturation and irreducible water. With the amount of information I have, I am forced to start with a vague estimate of petrophysical properties and subdivide the sequence into a small number of beds. This allows me to quickly obtain an initial model, from which I can focus on each bed separately by splitting them into smaller ones that will be adjusted and redefined afterward. Such method is often referred to as the ‘divide and conquer’ approach, a known technique to minimize the number of steps needed to obtain the final solution when sparse information is available. Concerning this case, I started with only four beds based on the variations observed in both density and compensated neutron logs. At first, I assumed that I was dealing with a siliciclastic sequence, but density and neutron results were shifted by an average of 22%. Assuming a carbonate formation provided a much closer fit (error reduced to 4%), which I confirmed afterward when I received more information about the sequence (Figure 4.12a).
Figure 4.12a: Field example No. 4: First iteration based on the carbonate assumption. Track 1: Depth track (ft). Track 2: Caliper (ft) and bed boundaries. Track 3: Field and simulated GR logs (gAPI). Track 5: Neutron (limestone porosity units) and Density (g/cm³) field logs, water (green) and hydrocarbon cross-over (yellow). Track 6: Neutron (limestone porosity units) and Density (g/cm³) simulated logs, water (green) and hydrocarbon cross-over (yellow).
At the second iteration, I subdivided the thicker layers to obtain a total of 12 layers. I did not have to redefine new layers from the beginning since I already had a close match initially. The second iteration was more time consuming, but it would have been more cumbersome if I skipped the first one (Figure 4.12b).

Once the model appears consistent enough, I consider the resistivity log and start readjusting porosities and water saturations. This is also a tedious process that could have been fine-tuned along with the remaining logs at the iteration level, but would have provided the ability to obtain a quick glimpse at the intermediary results longer.

Figure 4.13 shows the final outcome of this work after two iterations, and gives me a good assessment of the sequence. Resistivity simulations were performed only at this stage, which resulted in exhibiting a good match (3% error) to field logs. Note that both density and neutron logs had to be adjusted by increasing the salinity of connate water. Furthermore, the large cross-over between density and neutron logs indicated the presence of residual gas saturation. Moreover, the peak in the GR log at the depth of 2675 ft was not observed in the simulated logs since it correlated with in the caliper log; hence, this can be an error due to borehole enlargement. Throughout this field example, I realized that doing a series of iterative modeling yielded a better agreement between simulated and field logs.
Figure 4.12b: Second iteration applied on the previous model. Track 1: Depth track (ft). Track 2: Caliper (ft) and bed boundaries. Track 3: Field and simulated GR logs (gAPI). Track 4: Neutron (sandstone porosity units) and Density (g/cm$^3$) field logs, water (green) and hydrocarbon cross-over (yellow). Track 5: Neutron (limestone porosity units) and Density (g/cm$^3$) simulated logs, water (green) and hydrocarbon cross-over (yellow). Track 6: Sonic slowness (μs/ft).
Figure 4.13: Final model after the introduction of the resistivity log. Track 1: Depth track (ft). Track 2: Caliper (ft), bed boundaries, and petrophysical bed boundaries. Track 3: Field and simulated GR logs (gAPI). Track 4: Field and simulated Neutron (sandstone porosity units) logs. Track 6: Field and simulated Density (g/cm$^3$) logs. Track 7: Sonic slowness ($\mu$s/ft). Track 8: Neutron (sandstone porosity units) and Density (g/cm$^3$) field logs, water (green) and hydrocarbon cross-over (yellow). Track 9: Neutron (limestone porosity units) and Density (g/cm$^3$) simulated logs, water (green) and hydrocarbon cross-over (yellow).
4.2.5 Offshore Formation

The example has been previously considered by Angeles et al. (2009). This sequence describes a siliciclastic offshore reservoir, dated between upper Paleocene and lower Eocene. The well is situated under approximately 6500 ft of water.

When combining a high GR response with a clear separation between density and neutron logs (Figure 4.14a), I infer the existence of high volumes of shale in the formation. Hence, I used the dual-water model (Clavier et al., 1984) to calculate water saturation (free and clay-bound). The parameters I used for the model are \( a=1 \), \( m=1.9 \), and \( n=2.1 \).

Figure 4.14b shows the resulting simulated resistivity curves after simulating invasion with the Invasion Module. Note that the relatively large separation between the resistivity curves at the bottom half of the formation confirms the presence of mobile water. Therefore, the match had to be modified by adjusting the amount of irreducible water saturation. On the other hand, I chose to have a finer grid for the simulation of the top half of the sequence, which led to an average error of 3.5%.

Unlike the previous examples, I tried to match the resistivity logs prior to matching density and neutron logs; this resulted in a fairly larger error in the simulated density log (roughly 6.9%), while the simulated neutron log agreed with its corresponding field log (average error of 2.55%) (Figure 4.14a). Even though the simulated density log did not agree well with the field log, the error was not significant. Hence, changing the order of logs to be matched leads to approximately the same result. Finally, the simulated GR log matched the corresponding field log with an average error of 3.2%.
Figure 4.14a: Field and simulated logs for the offshore formation. Track 1: Bed boundaries, petrophysical bed boundaries and caliper (ft). Track 2: Lithology (fraction): quartz (yellow), biotite (brown), orthoclase (green), illite (grey), chlorite (pink), glauconite (dark green), shale water (dark blue), water (blue), oil (red). Track 3: GR (gAPI). Track 4: Density (g/cm³). Track 5: Neutron (sandstone porosity units). Track 6: Depth track (ft).
Figure 4.14b: Field and simulated logs for the offshore formation. Track 1: Bed boundaries, petrophysical bed boundaries and caliper (ft). Track 2: Lithology (fraction): quartz (yellow), biotite (brown), orthoclase (green), illite (grey), chlorite (pink), glauconite (dark green), shale water (dark blue), water (blue), oil (red). Tracks 6 to 10: Array Induction Two Foot Resistivity Tool from shallow to deeper depths of investigation (Ω.m).
CHAPTER 5

SUMMARY AND CONCLUSIONS

5.1 SUMMARY

I described a new method for interactive modeling and simulation of nuclear logs. Simulations were performed with a linear iterative refinement technique introduced by Mendoza (2009). The subsurface model under consideration consisted of horizontal beds with variable chemical compositions and volumetric concentrations of solid and fluid constituents. The use of core information, performing a full log analysis, and/or refining an initial guess by manually iterating a model is crucial to obtaining reliable simulations. Users enter constituents and their compositions via a choice palette. Subsequently, Schlumberger’s SNUPAR software is used to calculate nuclear properties necessary for the simulation of nuclear logs.

5.2 CONCLUSIONS

Testing of the software with synthetic, as well as field cases confirmed its applicability for the interactive matching of field logs. Despite difficulties and limitations associated with either unavailable data or uncertainty of some parameters, simulation methods used with the interactive procedure proved to be reliable.
In some situations, the trend of simulations obtained with the module was accurate but not the values. If such condition takes place for the case of gamma-ray or sonic logs, an adjustment is necessary in the spectral mineral values or sonic slowness.

The six synthetic cases indicated changes in nuclear simulations when making one modification at a time of the petrophysical properties of homogeneous beds. These modifications consisted of changing fluid/mineral composition, water salinity, porosity, adding an additional layer, or including thinly-bedded layers.

The five field examples described in this thesis revealed key factors about the approach to use when initializing a model:

- In the first example, I learned that the last log to be matched will have the highest error margin (ranging from 1.4% to 13.3%). Therefore, it is best to choose carefully the order of logs to be matched depending on their confidence level.

- In the second example, when dealing with a mixed siliciclastic-carbonate sequence primarily, the amount of limestone could be readily discerned from density, PEF, and neutron logs.

- In the third example, the availability of spectral GR logs greatly improved the petrophysical assessment of a formation; indeed, the thorium vs. potassium cross-plot was an efficient starting point to determine clay content.

- In the fourth example, I observed that when important information is missing about a formation, the ‘divide and conquer’ approach is the best option to perform the modeling process. It minimizes the numbers of steps needed to obtain the final solution. Moreover, using the iterative modeling technique results in a better match between simulated and field logs.

- In the last example, I used two approaches to solve the problem. The first one was to match the resistivity logs prior to matching neutron and density logs and the second
approach was to match the neutron and density logs before proceeding with the resistivity match. I observed that the error factor in the first approach was reduced by a factor of half compared to that of the second approach. Therefore, the order of matching logs is critical.

Furthermore, the options provided throughout the interactive modeling can narrow down the number of variables needed to initialize the simulations by testing one option at a time when current simulated results do not match field logs.

Even though simulated results are in close agreement with field logs, there were cases where the match in the PEF log was not as satisfactory as with other logs.

In this thesis, I introduced and successfully tested the concept of interactive modeling and interpretation of nuclear logs. I showed that numerical simulation and matching of field logs using fast modeling procedures is a practical method to improve the assessment of inferred static and dynamic formation petrophysical properties.
Appendix A

Detailed Inventory of Well Logs Available for the Field Cases

Table A.1 is a detailed inventory of well logs available for the case studies. It also identifies those wells with rock-core measurements. The terminology used to designate each well log in this table is explained in the nomenclature section. The last column of this table describes the availability of core analysis information.

<table>
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<tr>
<th>Case #</th>
<th>SP</th>
<th>Caliper</th>
<th>GR</th>
<th>Spectral</th>
<th>RHOB</th>
<th>NPHI</th>
<th>PEF</th>
<th>Resis</th>
<th>DT</th>
<th>Core</th>
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Table A.1: Detailed inventory of well logs available for this study.
Appendix B

Archie’s Equation and Summary of Parameters Considered for the Modeling of Water Saturation Curves

This appendix describes the parameters included in Archie’s equation. It also summarizes the parameters used for calculating water saturation.

In order to obtain $S_w$, $S_{xo}$ and $S_h$, we apply Archie’s equation, given by

$$
S_w = \left[ \frac{a}{\phi^m} \cdot \frac{R_w}{R_t} \right]^{n/m},
$$

where $a$ is tortuosity factor, $R_w$ is connate water resistivity, $\phi$ is porosity, and $m$ and $n$ are cementation and saturation exponents, respectively. In the carbonate and siliciclastic cases, the tortuosity factor is taken as 1 in equation 3.8 based on the type of lithology already observed in the description. Connate-water resistivity at reservoir conditions was estimated using a salinity of 6700 ppm, whereupon $R_w$ is equal to 0.23 $\Omega$.m at reservoir temperature.
Appendix C

Dual-Water Equation and Summary of Parameters Considered for the Modeling of Water Saturation Curves

This appendix describes the usage of the dual-water method for shaly sands (Clavier et al., 1984). In order to obtain $S_w$, I read $R_t$, $\phi$ and GR in the sand of interest, in a nearby shale, and in a clean sand. After calculating $C_{sh}$, correcting the porosities for shaliness, and calculating the non-shale porosity, I determine the total porosity of the nearby shale using

$$\phi_{sh} = \delta \cdot \phi_{D}^{sh} + (1 - \delta) \cdot \phi_{N}^{sh},$$  \hspace{1cm} (C.1)

where $0.5 \leq \delta \leq 0.9$. The bound-water fraction of the sand is then given by

$$S_b = C_{sh} \cdot \frac{\phi_{D}^{sh}}{\phi_{t}},$$  \hspace{1cm} (C.2)

with

$$\phi_{t} = \phi_{c} + C_{sh} \cdot \phi_{D}^{sh},$$  \hspace{1cm} (C.3)

and

$$R_b = R_{sh} \cdot \frac{\phi_{D}^{sh \cdot n}}{a},$$  \hspace{1cm} (C.4)

with $a = 1$, $m = 1.9$, and $n = 2.1$ for the field example No. 5. It follows that

$$\frac{1}{R_t} = S_w \cdot \frac{\phi_{D}^{m}}{a \cdot R_w} - \frac{S_w \cdot \phi_{D}^{m \cdot n} \cdot S_n}{a \cdot R_w} \cdot \left(1 - \frac{R_w}{R_b}\right),$$  \hspace{1cm} (C.5)

where $S_w$ is the dual-water saturation.
Nomenclature

\[ a \] : Tortuosity factor, dimensionless

\[ a_c \] : Thorium coefficient, dimensionless

\[ b_c \] : Uranium coefficient, dimensionless

\[ c_c \] : Potassium coefficient, dimensionless

\[ C_{sh} \] : Volumetric concentration of shale

\[ C_w \] : Volumetric concentration of NaCl in connate water, (ppm)

\[ DT \] : Field sonic log (slowness, us/ft)

\[ ECGR \] : Environmentally corrected gamma-ray, (API units)

\[ GR \] : Gamma-ray, (API units)

\[ K \] : Potassium concentration, (%)

\[ L_{m,\text{formation}} \] : Formation migration length, (ft)

\[ m \] : Cementation exponent, dimensionless

\[ M \] : Molecular weight, (g/mol)

\[ n \] : Saturation exponent, dimensionless

\[ NPHI \] : Neutron log, (water-filled porosity units, fraction)

\[ WBM \] : Water-base mud

\[ P_c \] : Critical pressure, (atm)

\[ PEF \] : Photoelectric factor log, (barn/electron)

\[ Phi_D \] : Density porosity, (fraction)

\[ Phi_N \] : Neutron porosity, (fraction)

\[ RHOB \] : Density log, (g/cm^3)

\[ R_b \] : Formation bulk resistivity, (Ohm-m)
\( R_{\text{cl}} \): Clay formation resistivity, (Ohm-m)

\( R_t \): True formation resistivity, (Ohm-m)

\( R_w \): Conrate water resistivity, (Ohm-m)

\( R_{w,a} \): Apparent water resistivity in shaly sand, (Ohm-m)

\( R_{xo} \): Flushed-zone formation resistivity, (Ohm-m)

\( \text{SP} \): Spontaneous potential, (mV)

\( S_b \): Bound-water fraction of sand, (fraction)

\( S_w \): Water saturation, (fraction)

\( S_{w,t} \): Total water saturation corrected for shale, (fraction)

\( T_c \): Critical temperature, (K)

\( Th \): Thorium concentration, (ppm)

\( U \): Uranium concentration, (ppm)

\( V_{P, \text{formation}} \): Sonic slowness model, (μs/ft)

Greek symbols

\( \Theta \): Contact angle between the fluid interface and the rock, (degrees)

\( \omega \): Acentric factor, dimensionless

\( \Delta t \): Sonic slowness, (μs/ft)

\( \Delta t_b \): Sonic slowness of pure bulk, (μs/ft)

\( \Delta t_f \): Sonic slowness of pure fluid, (μs/ft)

\( \Delta t_s \): Sonic slowness of pure solid, (μs/ft)

\( \Delta t_{sh,f} \): Sonic slowness of the shale fluid, (μs/ft)

\( \Delta t_{sh,s} \): Sonic slowness of the shale solid, (μs/ft)

\( \rho_a \): Simulated density, (g/cm³)

\( \rho_f \): Fluid density, (g/cm³)

\( \rho_{ma} \): Matrix density, (g/cm³)
\( \phi \) : Porosity, (fraction)
\( \phi_{DC} \) : Porosity obtained from bulk density log corrected for presence of shale, (fraction)
\( \phi_b \) : Bulk density log in a pure shale, (fraction)
\( \phi_e \) : Non-shale porosity, (fraction)
\( \phi_{cl} \) : Clay porosity, (fraction)
\( \phi_{NS} \) : Non-shale porosity, (fraction)
\( \phi_{NC} \) : Porosity calculated from neutron log corrected for presence of shale, (fraction)
\( \phi_N \) : Porosity calculated from neutron log without corrections for presence of shale, (fraction)
\( \phi_{Nh} \) : Neutron log response in a pure shale, (fraction)
\( \phi_{sh} \) : Total porosity of shale, (fraction)
\( \phi_{sh}^{D} \) : Density porosity of shale, (fraction)
\( \phi_{sh}^{N} \) : Neutron porosity of shale, (fraction)
References


"Log Interpretation Charts." Schlumberger Information Solutions, [http://www.slb.com/content/services/resources/books/log_charts/index.asp](http://www.slb.com/content/services/resources/books/log_charts/index.asp).


